THE DAY OF THE WEEK EFFECT IN BORSA ISTANBUL;  
A GARCH MODEL ANALYSIS

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ABSTRACT

The aim of this study is to investigate the Day of the Week Effect (DWE) in Borsa Istanbul BIST-100 Index. For this purpose, a dataset of closing prices of the firms was gathered from January 03.2005 to November 06.2015. The data were transformed to return series by taking logarithmic differences, and analyzed with GARCH (1,1) Model. According to the findings, although the coefficients representing the returns of Monday and Thursday are statistically significant, the returns of the trading days of the week are equal. Consequently, for the related period, DWE was not detected in BIST-100 Index.

Keywords: Day of the Week Effect, GARCH Model, BIST-100 Index.
1. Introduction

The subject of this study “anomalies in stock markets” is examined in the field of behavioral finance that is emerged opposed to the efficient market hypothesis (EMH). EMH-attracted great attention in 1970s- asserts that as the stock prices reflect all the current information of stock market, future returns of these assets will not be predicted. Investors are rational and able to access to information. Hence, there will not be any contingency, and investors always make the right decision. The hypothesis started to be questioned in 1980s, because the fluctuations of the prices could not be explained adequately (Shiller, 2003).

Behavioral finance emerged to clarify these anomalies. Some researchers assert that people cannot always make right decisions,and psychological and sociological factors can affect their decisions. People can change their decisions according to these factors and in certain times they may tend to behave jointly. If an observation cannot be explained by the assumptions of EMH and cannot be explained logically it is so called “Anomaly”. Anomalies are commonly examined in literature under 3 titles: calendar anomalies, firm anomalies, and prize anomalies.

Researches on anomalies lead investors to develop strategies and gain over-expected returns. If an anomaly defined in the stock market, investors invest regarding the certain times that the anomalies detected and gain profit. As the behavioral finance attracted attention, calendar anomalies become the most researched anomaly type. The first research in the field was conducted in USA. Osborne (1962), Cross (1973), Roseff & Kinney (1976), French (1980), Gibbons & Hess (1981), and Ariel (1987) are the first researchers examined the calendar anomalies.

The subject of this study is to investigate the day of the week effect—a widely researched anomaly type- in Borsa Istanbul BIST-100 Index. In accordance with this purpose, the closing prices of the stocks that were traded in BIST-100 Index between the periods of 03.01.2005–06.11.2015 were taken as dataset. The closing prices transformed to return series by taking logarithmic difference and analyzed with GARCH (1,1) Model.

2. Literature Review

2.1. Efficient Market Hypothesis

Efficient Market Hypothesis (EMH) was introduced by Fama in 1970. According to this hypothesis, the efficiency means that stock prices reflect all the current information and investors consider this information in their investment decisions. Stock prices exhibit a random distribution. That relationship between information and price—the price change according to every new information- leads to the fact that the future asset prices cannot be predicted. According to the Random Walk Theory the stock prices reflect merely the current day’s information and are independent for the information spreads rapidly (Fama, 1970; Malkiel, 2003).

The assumptions of the EMH are (Fama, 1970):

- Investors are rational and always take the right decisions.
- Investors have full information.
- Investors search for maximizing their benefit.
As the Fama (1970) revealed exciting results, anomalies based on little dependencies were observed in his work (Schiller, 2003). Fama & French (1998) examined the stock market returns in short and long periods and defined positive correlation in short term and negative correlation in long term between the current returns and past returns. In his 1998 work Fama examined whether stock prices react to information or not, and found that although unexpected returns, stock splits dividend actions, mergers, exchange listings, and announcements about primary market offerings lead to mobilization in stock prices, investors will not be able to gain abnormal returns, and explained the market condition in terms of reflection of prices as:

- All the participants can access to information at no cost,
- There are no transaction costs,
- All the participants agree that the stock prices reflect the information in the current state and in the future.

Fama (1998) asserts that the stated conditions are adequate but not necessary, and the efficiency of market will be provided as adequate number of investor access to information.

Malkiel (2003) defined “efficient market” as the markets investors will not be able to gain returns above the average unless they take risk above the average, and supports the view that stock markets do not have memory. Schwert (2003) stated that many prediction models disappear as they published in finance literature. The view that “prediction of stock returns” will lead investors to the aim of limitless profit. Hence, the market becomes a “money machine” that produces wealth. As such a situation is not possible in a stable economy, investor foster stock market returns to follow EMH (Timmerman & Granger, 2004).

Psychologist Daniel Kahneman won a Nobel Prize in economics with Amos Tversky on their groundbreaking work “Prospect Theory: An Analysis Of Decision Under Risk” Robert Shiller, Matthew Rabin, Sendhil Mullainathan, Esther Duflo and Raj Chetty are the researchers that won Nobel Prizes for their work in behavioral finance Robert Shiller receives the Nobel Prize in economics for his work on asset bubbles and “irrational exuberance” in the stock market, and ironically he also shared the award with Eugene Fama, father of the “efficient-market hypothesis,” and another financial economist, Lars Hansen (Finkle, 2017).

2.2. Stock Market Anomalies

By the 21st Century, many researchers and statisticians supported the view that stock market returns are predictable to some extent, and new generation scientists started to conduct researches that propose psychological and behavioral factors are also affect stock market prices (Malkiel, 2003). Neglecting the freewill is one of the critiques directed to EMH. Investors consider not only economic and financial indicators but also their inner world, past experiences, and perception of opportunities while making investment decisions (Taner & Akkaya, 2005). In today’s financial markets the incentives of fatalism, overconfidence, and joint action are effective (Cross et al., 2005).

Behavioral finance was developed in order to clarify the issues that EPH cannot explain, is a branch of finance that finance, psychology, and behavioral sciences are relatedly considered
Behavioral finance focuses on investors’ irrational behaviors and psychological assumptions. If investors that are affected by sociological and psychological factors, they may change their decisions, or may overreact or underreact in some conditions. If EPH cannot explain that condition than it is called anomaly. Behavioral finance aims to identify the anomalies and to find out the reasons that lead to anomaly. As the anomalies are identified, investors will be able develop investment strategies.

Stock market anomalies are defined as the situations that cannot be explained by EMH and emerged due to the conditions as season, holiday, and liquidity preferences (Mbululu & Chipeta, 2012). There are many types of stock market anomalies that are defined by researches but anomalies are generally identified under three titles: Calendar anomalies, firm size anomaly, and price anomaly. The types of anomalies that are mostly observed and their definitions are represented on Table 1.

Table 1: Stock Market Anomalies

<table>
<thead>
<tr>
<th>Anomaly Types</th>
<th>Definitions</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>1. Calendar Anomalies</strong></td>
<td></td>
</tr>
<tr>
<td>- The Day of the Week Effect (DWE)</td>
<td>The returns of each trading day of the week are not equal. Monday effect -lower and negative returns on Mondays-and Friday effect -higher returns on Fridays- are the most observed DWE types in literature (Cross, 1973; Miralles Marcelo &amp; Mirales Quiros, 2002; Brounen &amp; Ben Hamo, 2009)</td>
</tr>
<tr>
<td>- January Effect</td>
<td>Relatively higher returns on January among the other months of the years (Wachtel, 1942; Rozeff &amp; Kinney, 1976; Moosa, 2007).</td>
</tr>
<tr>
<td>- The Turn of the Month Effect</td>
<td>Relatively higher returns on the first four days and last four days of the month (Lakonishok &amp; Smidt, 1988; Ziemba 1991; Cadsby &amp; Ratner, 1992).</td>
</tr>
<tr>
<td>- Holiday Effect</td>
<td>The rise of the stock prices the day before the holiday (Fields, 1934; Meneu &amp; Pordo 2004; Marrett &amp; Worthington, 2007).</td>
</tr>
<tr>
<td><strong>2. Firm-size Anomalies</strong></td>
<td></td>
</tr>
<tr>
<td>- Over-reaction</td>
<td>The negative correlation among the firm size and average returns (Banz 1981; Keim, 1983; Balint, 2012).</td>
</tr>
<tr>
<td><strong>3. Price Anomalies</strong></td>
<td></td>
</tr>
<tr>
<td>- Over-reaction</td>
<td>The under-reaction of investors to the announcements about stock market prices in the period of 1 to 12 months (De Bondt &amp; Thaler, 1985, 1987)</td>
</tr>
<tr>
<td>- Under-reaction</td>
<td>The long-term (three to five years) over-reaction of investors to especially dividend announcements (Barberis, Shleifer &amp; Vishy, 1998)</td>
</tr>
</tbody>
</table>
Besides these 3 types of anomalies there are also anomaly types based on:

Price-Earnings (P/E) ratio: “P/E ratios are indicators of the future investment performance of a security. Proponents of this price-ratio hypothesis claim that low P/E securities will tend to outperform high P/E stocks” (Basu, 1977: 663).

The Price Earnings-Growth ratio: PEG ratio \( \frac{\text{PE}}{\text{Short Term Earnings}} \) “has become a popular means of combining prices and forecasts of earnings and earnings growth into a ratio that is used as a basis for stock recommendations (implicitly for comparing expected rates of return)” (Easton, 2004: 74).

2.2.1. The Day of the Week Effect (DWE)

The most observed anomaly type in stock market anomalies is ‘the day of week effect’ - expresses the situation that the returns of each trading day of the week are not equal (Tunçel, 2007).

Osborne (1962), Cross (1973), Rozeff & Kinney (1976), French (1980), Gibbons & Hess (1981), Ariel (1987) are the first researchers that examined DWE in United States. Osborne (1962) found evidences related to specific times of days, weeks and the year. Osborne (1962) defined non-random movements in Standart & Poors Composite Index (S&P). French (1980) defined a day of week effect and weekend effect in S&P. Gibbons and Hess (1981) observed that the returns of stocks and treasury bonds were not constant through the week and defined that the returns on Mondays are low or negative.

After these researchers found evidence about the day of week effect in USA, researchers started to search for DWE worldwide. Miralles Marcelo & Miralles Quiros (2002) defined the existence of DWE in Lisbon Stock Exchange. Kiymaz & Berument (2003) conducted a research on Canada, Germany, Japan, United Kingdom, and USA Stock Exchanges and defined DWE in different days of the week in these markets. Sakalauskas & Kriksciuniene (2007) searched for DWE in developing countries. For the analyze results conducted with the data of Vilnius OMX Index, it is defined that DWE was in tendency to disappear. Brounen & Ben Hamo (2009) conducted a research with the data of prominent stock exchanges worldwide and defined anomalies on stock prices as higher returns on Fridays and lower on Mondays. Angelovska (2013) searched for calendar anomalies in Macedonian Stock Exchange and defined a DWE on Wednesdays.

Especially for the last two decades some researchers as Kamara (1997), Dimson & Marsh (1999), Brusa et. al. (2000), Mehdian & Perry (2002) found evidences in terms of anomalies were disappearing (Brounen & Ben Hamo, 2009).
2.2.2. The Day of the Week Effect in Borsa Istanbul.

Istanbul Stock Exchange (ISE) was founded in December 1985. ISE and Istanbul Gold Exchange was merged under Borsa Istanbul in April 2013. BIST100 Index is the basic index for Istanbul Share Market. It consists of 100 shares selected from the firms that are traded in Star Market and Main Market, real estate investment trusts and venture-capital trusts.

Many researches carried out to define DWE effect in Borsa Istanbul. Karan (1994), Aydoğan (1994), Balaban (1995), Bildik (2000), Özmen (1997), Demirer & Karan (2002), Karan (2002), Karan & Uygur (2001)’s findings commonly indicate that the returns on Fridays are higher than the other trade days of the week, and though they are not statistically significant, negative returns on Mondays and Tuesdays, and Atakan (2008) defined negative returns on Mondays. Karan (2001) reviewed the recent studies on Istanbul Stock Exchange (ISE) and supported that ISE was not an efficient market. Metin, Muradoğlu & Yazıcı (1997) conducted Research on ISE in the period of 1988-1996 and observed both Monday and Friday Effects. Ergül et. al. (2008) examined ISE composit-100 Index for the period between 1988 and 2007 and found that it is possible to gain daily abnormal returns for he market is not efficient. Heşpen (2012) searched for anomalies in ISE Real Estate Investment Trust (REIT) Index and defined a Monday Effect. Aksoy & Ulusoy (2015) examined the return and volatility behavior in REIT and BIST-100 Indexes in the period from 2000 to 2014 and defined that calendar anomalies still exists for both indexes, solely DWE for returns disappeared in BIST-100 Index.

Researches on DWE in BIST broadly support the view that BIST is an inefficient market. Based on these findings, defining the recent situation of the market was aimed in this research. For this purpose, a recent period of 03.01.2005 - 06.11.2015 was decided on, and basic index -BIST 100- was selected to analyze.

3. Methodology

3.1. Data

The closing prices of the stocks was used in this research that was traded in BIST-100 Index between the periods of January 3, 2005 – November 6, 2015. The data was gathered from the official web site of Central Bank of Turkish Republic. The return series was used in analyze evaluated by taking logarithmic differences of closing prices. The purpose of taking logarithmic differences is to make the data stationary (Miralles-Marcello & Miralles-Quiros, 2002). The logarithmic differences of 2058 observations were calculated as follows:

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2 Star Market 1st group: Stock market value ≥ 250.000.000 TL, total market value ≥ 1.000.000. 000 TL; nominal value / min. capital rate =5%, equity / capital rate ≥ 0,75 Star Market 2nd group: Stock market value ≥ 100.000.000 TL, total market value ≥ 400.000.000 TL, nominal value/min capital rate = 10;% equity/capital rate ≥ 1
3 Main Market 1st group: Stock market value ≥ 50.000.000, nominal value /min. Capital rate = 15% equity/capital rate ≥ 1 Main Market 2nd group: Stock market value ≥ 25.000.000, nominal value / min. capital rate = %25, equity / capital rate ≥ 1,25
\[ R_t = \ln \frac{I_t}{I_{t-1}} \]  

(1)

\( R_t \) = Return of BIST-100 index between two closing time on day \( t \).
\( I_t \) = Closing price of BIST-100 index on day \( t \).
\( I_{t-1} \) = Closing price of BIST-100 index on day \( t-1 \).

The descriptive statistics of return series are displayed on Table 2

<table>
<thead>
<tr>
<th>Table 2: Descriptive Statistics of Return Series</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean</td>
</tr>
<tr>
<td>Median</td>
</tr>
<tr>
<td>Maximum</td>
</tr>
<tr>
<td>Minimum</td>
</tr>
<tr>
<td>Std. Dev.</td>
</tr>
<tr>
<td>Skewness</td>
</tr>
<tr>
<td>Kurtosis</td>
</tr>
<tr>
<td>Jarque-Bera</td>
</tr>
<tr>
<td>Probability</td>
</tr>
<tr>
<td>Sum</td>
</tr>
<tr>
<td>Sum sq. dev.</td>
</tr>
<tr>
<td>Observations</td>
</tr>
</tbody>
</table>

The statistics on Table 1, indicates that return series exhibit normal distribution (JB statistics is significant on level 0.01). According to null hypothesis series exhibit normal distribution. The hypothesis is rejected. Hence, return series do not exhibit normal distribution. This situation is related especially to the high kurtosis coefficient (Silva, 2010).

3.2. Model

Autoregressive Conditional Heteroskedastic (ARCH) Model is the process introduced by Engel (1986) allows the conditional variance to change over time as a function of past errors leaving the unconditional variance constant. As ARCH offers a solution for the assumption of constant variance, it has some conflicts that often will lead to violation of the non-negativity constraints derived from estimating a totally free lag distribution. In order to solve this problem Bollerslev (1986) developed Generalized Regressive Conditional Heteroskedasticity (GARCH) Model that is a natural generalized form of ARCH (Bollerslev, 1986).

Heteroskedasticity indicates “a formal model of the process that generating the different variances, these difficulties are easily eliminated by performing an appropriate linear transformation on the data based on this model. However, “even when such model is available, it may be incorrect” (White, 1980:817). As heteroskedasticity is a commonly observed
behavior in time series, Ordinary Least Squares (OLS) Methodology does not operate efficient under heteroskedasticity, and the findings are not reliable. For this reason, in this research it is preferred to employ GARCH (1,1) - the simplest and often very useful form of GARCH as Bollerslev (1986) asserted.

Main regression model with 5 dummies was constructed in order to test DWE, as follows:

\[
R_t = \sum_{i=1}^{5} \alpha_i D_{it} + \varepsilon_t
\]  

(2)

- **\( R_t \)**: The average daily return
- **\( \alpha \)**: The average daily return of each trading day
- **\( D_i \)**: Dummy variables, representing the trading days of the week (\( D_1 \) is equal to 1 on Mondays, 0 for all other days; \( D_2 \) is equal to 1 on Tuesdays, 0 for all other days; \( D_3 \) is equal to 1 for Wednesdays and 0 for all other days; \( D_4 \) is equal to 1 for Thursdays and 0 for all other days, \( D_5 \) is equal to 1 for Fridays and 0 for all other days).
- **\( \varepsilon_t \)**: Error term

Dummy variables -represented as \( D_i \) in the equation (2) are independent variables which take the value of either 0 or 1. Just as a, a dummy variable is a numeric stand-in for a qualitative fact or a logical proposition” (Garavaglia, & Sharma, 1998:43).

Error term -represented as \( \varepsilon_t \) in the equation (2) and also called as “residual”- represents “the difference between the actual value of the dependent variable and the estimated value of the dependent variable at the regression equation” (Zikmund, 2000:519).

The regression model is formed to test the following hypothesis indicating that the average returns of each trading day are equal.

\[
H_0: \alpha_1 = \alpha_2 = \alpha_3 = \alpha_4 = \alpha_5
\]

At first, Ordinary Least Squares (OLS) Methodology was applied to the model, but it was defined that error terms exhibit heteroskedasticity. To eliminate this problem, following GARCH (1,1) Model was formed:

\[
R_t = \sum_{i=1}^{5} \alpha_i D_{it} + \varepsilon_t
\]  

(3)

\[
\varepsilon_t | \varphi_{t-1} : N(0,h_t)
\]  

(4)

\[
h_t = \gamma_0 + \gamma_1 \varepsilon_{t-1}^2 + \gamma_2 h_{t-1}
\]  

(5)
**R$_t$**: The average of BIST-100 index between two closing time on day $t$.

**$\alpha_i$**: The average return of each trading day of a week.

**D$_i$**: Dummy variables, representing the trading days of the week (D$_1$ is equal to 1 on Mondays, 0 for all other days; D$_2$ is equal to 1 on Tuesdays, 0 for all other days; D$_3$ is equal to 1 for Wednesdays and 0 for all other days; D$_4$ is equal to 1 for Thursdays and 0 for all other days, D$_5$ is equal to 1 and 0 for all other days).

**$\varepsilon_t$**: Error term

**$h_t$**: Conditional variance

**$h_{t-1}$**: Lagged conditional variance

The equation represents that error terms exhibit conditional distribution at the dataset of $\phi$ on “$t-1$” time, and the conditional variance is depended to lagged square of error terms and lagged conditional variance.

4. Findings

4.1. GARCH (1,1) Model findings on DWE effect in BIST-100 index

The GARCH (1,1) Model was analyzed by Eviews 8.0 software. It is defined that the problem of heteroskedasticity is eliminated, and the model do not include autocorrelation. The findings of the analysis are displayed on Table 3.

<table>
<thead>
<tr>
<th>Variables</th>
<th>Coefficients</th>
<th>Statistics z</th>
<th>p values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Monday (D$_1$)</td>
<td>0.001531</td>
<td>2.454101</td>
<td><strong>0.0141</strong></td>
</tr>
<tr>
<td>Tuesday (D$_2$)</td>
<td>0.000729</td>
<td>1.062741</td>
<td>0.2879</td>
</tr>
<tr>
<td>Wednesday (D$_3$)</td>
<td>0.001006</td>
<td>1.518616</td>
<td>0.1289</td>
</tr>
<tr>
<td>Thursday (D$_4$)</td>
<td>0.001775</td>
<td>2.846515</td>
<td><strong>0.0044</strong></td>
</tr>
<tr>
<td>Friday (D$_5$)</td>
<td>0.000923</td>
<td>1.308997</td>
<td>0.1905</td>
</tr>
</tbody>
</table>

*significant at 0.01 % level. **significant at 0.05 % level

Table 3 indicates that the returns on Mondays (D$_1$) have statistically significant effect on average returns ($R$) at the level of 0.05, and on Thursdays (D$_4$) at the level of 0.01. These findings suggest that there may be Monday and Thursday Effects on BIST-100 Index for the related period.

4.2. Wald Test Findings

The Wald test statistics is the estimation of unrestricted regression without imposing the coefficient restrictions specified by the null hypothesis. It measures how close the unrestricted estimation satisfies the restrictions under the null hypothesis (Ergün&Göksu, 2013: 138). The
following hypothesis was tested by Wald Test to examine the existence of DWE in BIST-100 Index, and the results are presented on Table 4.

\[ H_0 = \alpha_1 = \alpha_2 = \alpha_3 = \alpha_4 = \alpha_5 \]  

(6)

The null hypothesis represents that the returns of each trading day of the week are equal.

Table 4: WALD Test Findings

<table>
<thead>
<tr>
<th>Test Statistic</th>
<th>Value</th>
<th>df</th>
<th>Probability</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chi-square</td>
<td>1.872846</td>
<td>4</td>
<td>0.7591</td>
</tr>
</tbody>
</table>

According to Wald Test results, \( H_0 \) hypothesis was confirmed at the significance level of 0.05 (0.7591<0.05). Hence, average returns of each trading day of the week are equal to each other, and BIST-100 is an efficient market in terms of DWE for the related period.

5. Conclusion

DWE, one of the most researched anomaly types, is examined in this research. According to the findings of GARCH (1,1) Model analysis, it is defined that BIST-100 index is an efficient market. This result does not support the findings of the researches that returns on Mondays are negative and lower and returns Fridays are higher than the other trading days of the week (Ergül et. al., 2008, Abdioğlu & Değirmenci, 2013), returns of Mondays are lower than other trading days of the week (Atakan, 2008; Hepşen, 2012; Konak & Kendirli, 2014), returns on Fridays are higher than the other trading days (Karan, 1994; Aydoğan, 1994; Balaban, 1995; Bildik, 2000; Özmen, 1997; Demirer & Karan, 2002; Karan & Uygur, 2001; Karan 2002), returns of Tuesdays are lower and negative and returns of Fridays are higher than other trading days of the week (Muradoğlu & Oktay, 1993; Bildik, 2000). Though few, there are also researches that DWE was not detected (Aybar, 1993; Tunçel, 2007; Başdaş, 2011).

As a more recent period was examined in this research, the result can be interpreted as DWE is getting disappeared in BIST-100 index. In international literature, there are also researches as Dimson & Marsh (1999), Kamara (1997), Brusa et. al. (2000), Mehdian & Perry (2000) asserting that Monday Effect has disappeared in USA (Brounen & Ben Hamo, 2009).

The future researches that consider different indexes and other calendar anomaly types will introduce more evidence about the efficiency of BIST.

References


